

Estimation of Tumor Tracer Kinetics Employing a Novel Cross-Voxel Exchange Model

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INTRODUCTION

- Pharmacokinetic models, in conjunction with DCE-MRI, allow the estimation of transport properties of drugs in tumor tissue.

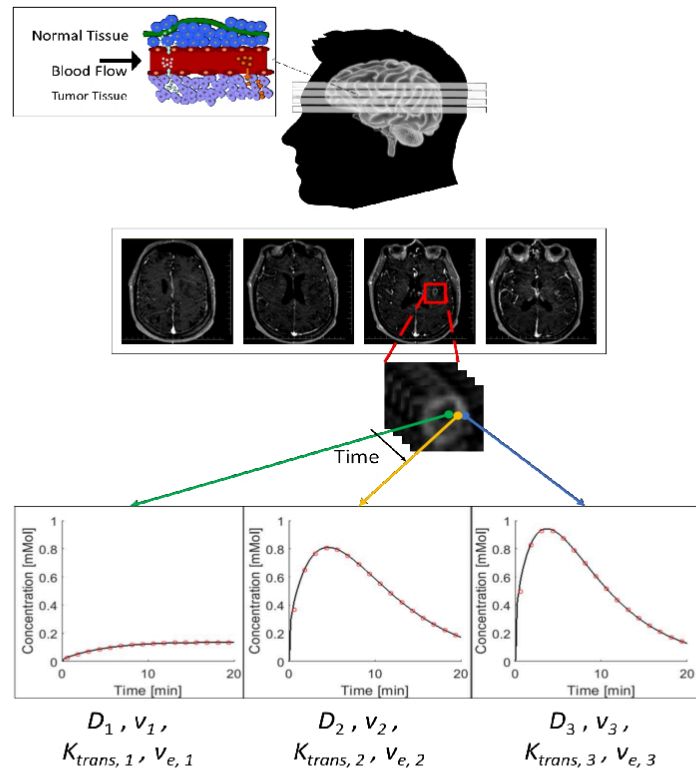


Figure 1: DCE-MRI and DCE-CT images are time-sequenced scans that record the extravasation of a CA from the intravascular network into the extravascular space. The change of tracer concentration over time is captured in an array of discrete elements, voxels.

- Drugs are transported to the tumor tissue via 3 mechanisms: diffusion, convection and extravasation.

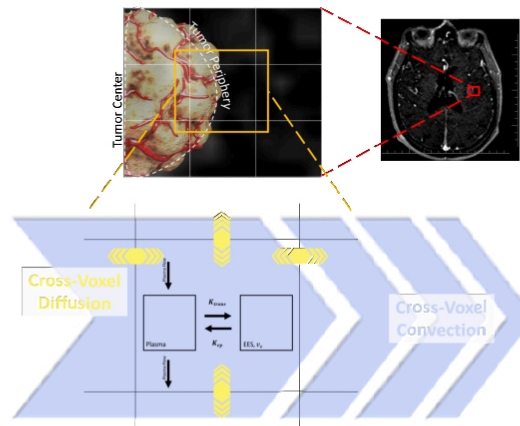


Figure 2: The variation of concentration in each voxel illustrates the exchange of tracer within a voxel (extravasation) as well as a cross-voxel exchange (convection and diffusion) in tumor tissue. The fitting of transport models to these time-concentration curves allows the quantification of transport parameters.

- Tofts Model (TM), most commonly used pharmacokinetic model. The application of TM assumes no cross-voxel transport of tracer leading to the misinterpretation of tracer perfusion in tumors^{1,2}.

AIM

- Develop the Cross-Voxel Exchange Model (CVXM) to describe extravascular diffusion and convection, in addition to the exchange of tracer between the blood vessels and tumor tissue.
- Investigate the impact of cross-voxel transport on the interpretation of Tofts' perfusion parameters using *in-silico* datasets.
- Test the feasibility of using CVXM in a practical setting. Derive transport parameters from DCE-MRI of a TS-415 human cervical carcinoma xenograft by using TM and CVXM.

MATHEMATICAL MODELLING

Development of the Cross-Voxel Exchange Model (CVXM)

$$\frac{\partial c(\mathbf{r}, t)}{\partial t} + \nabla \cdot \mathbf{j}(\mathbf{r}, t) = \Lambda(\mathbf{r}, t)$$
$$\mathbf{j}(\mathbf{r}, t) = c(\mathbf{r}, t) \mathbf{v}(\mathbf{r}) - D \nabla c(\mathbf{r}, t)$$
$$\Lambda(\mathbf{r}, t) = K_{ext}(C_p(t) - c(\mathbf{r}, t))$$

Convection Diffusion Exchange blood vessels-tissue

c local concentration of tracer in the extracellular extravascular space
 C_p concentration of the tracer in plasma
 v velocity of fluid flow in the tumor tissue
 D diffusivity of the tracer in the tumor tissue
 K_{ext} extravasation parameter function of the capillary permeability in at the boundary of capillaries (0 otherwise)

ABBREVIATIONS

CVXM	Cross-Voxel Exchange Model
DCE-MRI	Dynamic Contrast Enhanced Magnetic Resonance Imaging
TM	Tofts Model

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IN-SILICO TESTING

- Simulations: Data generated using CVXM with varying diffusion, convection and extravasation parameters.

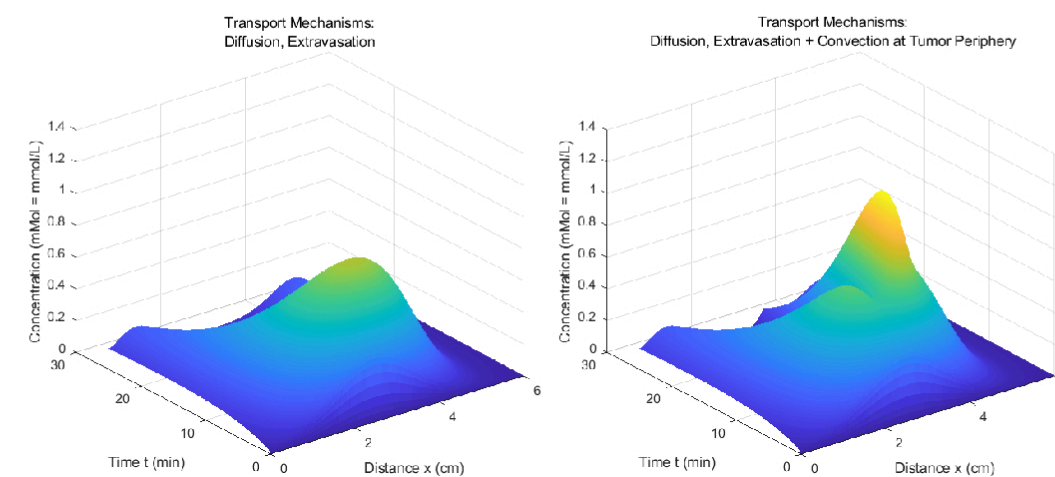


Figure 3: Numerical solutions of tissue concentration for Tissue Models.

- Fitting: TM fitted to the simulated data to produce an estimate of Tofts' perfusion parameters K_{trans} and v_e .

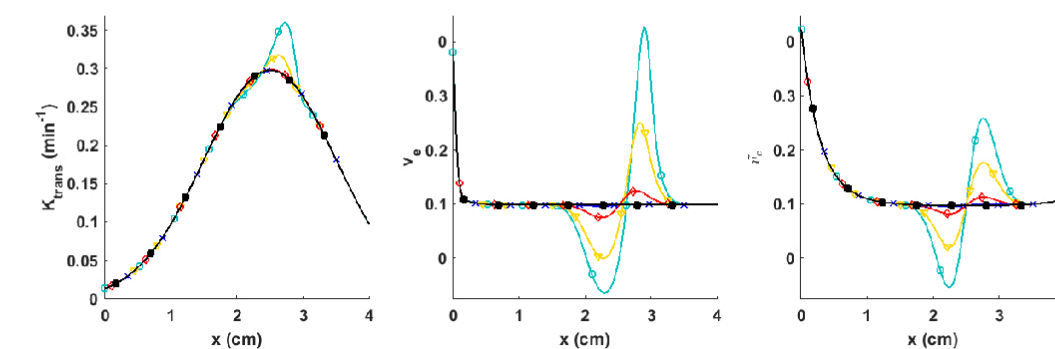


Figure 4: Results of fitting TM to the simulated data. Left: plots comparing the fitted K_{trans} profiles to the input parameters K_{ext} (black line). Middle: corresponding plots of the fitted v_e profiles. Right: v_e plots generated using equation developed to predict the impact of cross-voxel transport on Tofts' v_e . Colors correspond to the fitting results of data simulated with varying velocity profiles with peak $v = 0$ (●), 0.1 (■), 1 (○), 5 (▲) and 10 (☆) $\mu\text{m/s}$.

CONCLUSIONS

CVXM, paired with DCE-MRI, allows for a more accurate understanding of physical mechanisms driving tracer transport in the tumor microenvironment
» » » Better informed and more personalized treatment choices.

Tofts' extravasation parameters reflect the effects of inter-voxel diffusion and convection, even though TM does not include these effects (*in-silico* testing).

Fitting TM and CVXM to DCE-MRI data of TS-415 cervical carcinoma xenografts reveals that CVXM parameters are a more accurate representation of transport parameters in tumors.

PRE-CLINICAL TESTING

- Tumor Model: TS-415 human cervical carcinoma³.
- Data Acquisition: DCE-MRI recorded using a 1.5-T whole body scanner (Signa, General Electric) over a period of 15 min³.
- Model fitting: TM and CVXM fitted to DCE-MRI data to produce an estimate of TM and CVXM parameters.

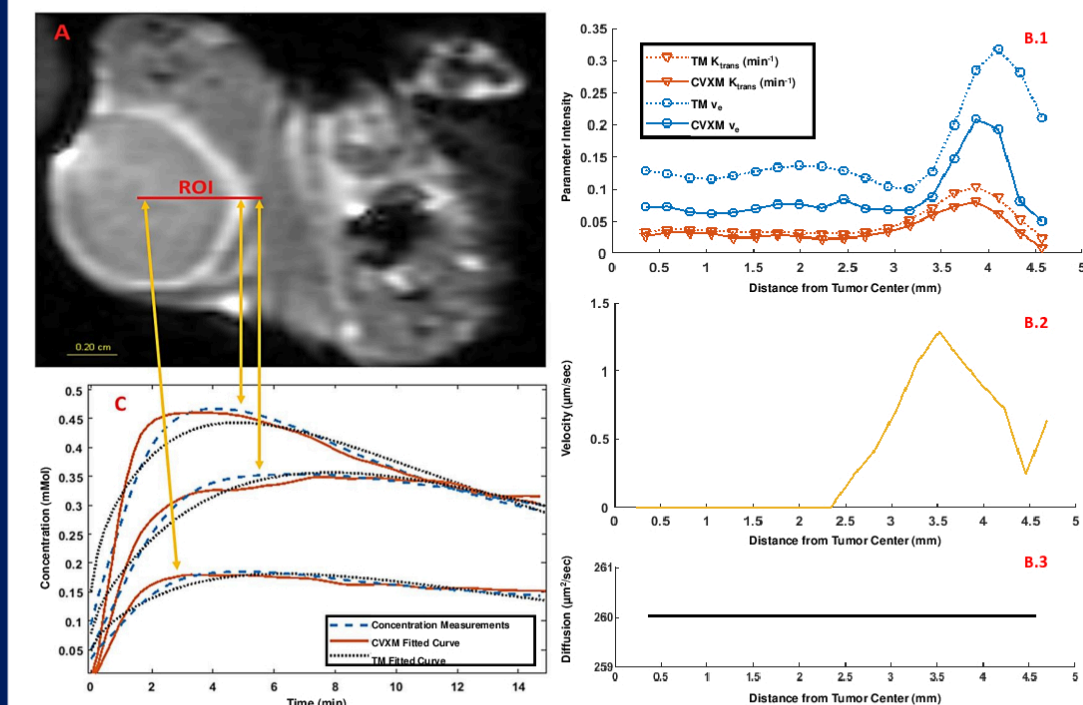


Figure 5: Transport parameters derived from DCE-MRI of a TS-415 human cervical carcinoma xenograft by using TM and CVXM.

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