

The Correction Term of A Three-Pool Kinetic Model for In Vitro Anaerobic Glycolysis Under

Authors, C. Hsieh^{1,2}, K Lu^{2,3}, G Lin^{2,3}, C. Wu⁴, F Chen^{4,5}

1 Institute for Radiological Research, Chang Gung University, Taoyuan, TW, ROC 2 Imaging Core Lab., Chang Gung Memorial Hospital, Linkou, Taoyuan, TW, ROC 3 Dept. of Medical Imaging and Intervention, Chang Gung Memorial Hospital, Linkou, Taoyuan, TW, ROC 4 Radiation Biologay Core Lab., Chang Gung Memorial Hospital, Linkou, Taoyuan, TW, ROC 5 Dept. of Medical Imaging and Radiological Sciences, Chang Gung University, Taoyuan, TW, ROC



INTRODUCTION

In Oncology, the Warburg effect is a form of modified cellular metabolism based on aerobic fermentation found in cancer cells, which tend to favor anaerobic glycolysis rather than the oxidative phosphorylation pathway which is the preference of most other cells in the body. The activity of anaerobic glycolysis reaction may be detected in-vitro or in-vivo by ¹³C MRS of hyperpolarized (HP) substrates. The HP signal of ¹³C substrates can be boosted by the technique called Dynamic Nuclear Polarization in the commercial polarizer.

AIM

The dynamic signals from HP substrates and products have been fitted to a number of mathematical models to determine metabolic reaction rates [1]. However, the acquisition time period in HP ¹³C experiment may not reach the steady-state status between HP ¹³C pyruvate and cells. Here, we have introduced a correction term, the metabolic reaction rate in anaerobic glycolysis as a function of time, into the traditional model to verify the feasibility.

METHOD

- Model: use three compartment bidirectional model to fit the conversion rates of pyruvate to lactate, and lactate to pyruvate in the intracellular region. Figure 1 and Equations have explained this model in detail.
- Hyperpolarization: the HP ¹³C signal was generated by a commercial polarizer, GE SPINLab.
- **In-Vitro experiment**, THP1 cells (6x10⁷) were in 9 ml medium. The HP ¹³C pyruvate, 1 ml, was poured into this medium. One group of these cells were exposed by radiation (15 Gy). The other group of these cell were not exposed by radiation. Two sets of in-vitro experiments were conducted.
- **Data acquisition:** HP ¹³C signal was acquired by the generic pulse-and-acquire MRS at GE 3T with MNS research package.
- **Data post-processing:** the raw data was reconstructed, apadization, phase correction, and background subtraction by GE Sage software. T₁ values of ¹³C Pyruvate also needed to be calculated by the least square fit before we input ¹³C pyruvate and lactate data into our model

RESULTS

- Adding the correction term in our model has fitted the ¹³C lactate in cell experiments is comparable to the traditional model without the correction term in Fig. 2(b).
- 2. In Figure 2(a), pyruvate data among experiment, our model and traditional model were overlapped. The scale comparison between Fig. 2 (a) and Fig. 2(b) in the y-axis (signal) reflected small amount of HP Lac. conversion to HP Pyr. Thus, the correction term of our model in ¹³C pyruvate did not reveal the large difference compared to the traditional model.
- 3. Table 1 showed the chemical reaction rate between radiation and non-radiation groups. The value in the radiation group was lower than that in the non-radiation group. This result reflected that lactate production after radiation was less.
- The uncertainty of fitted results in Table 1 was about 30%.

Method: Model Description

[1,2]. T_{delay} reflects the degree of reaction rate.

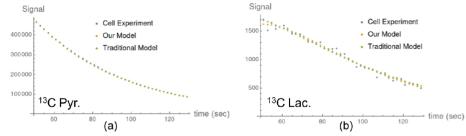
 $K_{pl}(t) = K_{pl,f} \left(1 - e^{-t/T_{delay}} \right)$

 $P'_{EXT}(t) = K_{ie}P_{INT}(t) - K_{ei}P_{EXT}(t) - \rho_{P,EXT}P_{EXT}(t) - \cdots - - (1)$

 $L'_{INT}(t) = K_{pl}(t)P_{INT}(t) - K_{lp}(t)L_{INT}(t) - \rho_{LINT}L_{INT}(t) - \cdots - (3)$

 $P'_{INT}(t) = K_{ei}(t)P_{EXT}(t) - K_{ie}P_{INT}(t) + K_{lp}(t)L_{INT}(t) - K_{pl}(t)P_{INT}(t) - \rho_{P,INT}P_{INT}(t)(2)$

model. Time, t, was initiated at the moment of HP pyruvate mixture with the cells.



model (orange), and traditional model (green).

Fig. 1 Schematic of pyruvate uptake and metabolism. Illustration of parameters that need to be included in three compartment

bidirectional modeling pyruvate delivery and conversion. These include K_{el} ,the rate of transfer from extracelluar space (e) to

intracellular space (i), K_n, the conversion rate from pyruvate to lactate in the intracellular space, K_n, the conversion rate from

actate to pyruvate in the intracellular space. "P_{EXT}" extracellular pyruvate. "P_{INT}" intracellular pyruvate. "L_{INT}" intracellular lactate.

In this three-pool bidirectional model, we consider that $P_{EXT}(t)$ is the substrate outside the cellular

membrane, $P_{INT}(t)$ is the same substrate inside the cellular membrane, and $L_{INT}(t)$ is the product in

the cytoplasm. Figure 1 is the schematic diagram of a bidirectional three-pool model. Eqs. (1)-(3),

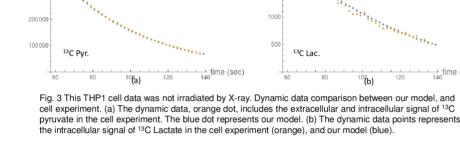
model. K_{plf} and K_{lnf} are the constant conversion rates, which have been used in the past literature

 $K_{lp}(t) = K_{lp,f} \left(1 - e^{-t/T_{delay}} \right)$

We assume that the effective relaxivity, $\rho_{P,EXT}$, $\rho_{P,INT}$, and $\rho_{L,INT}$ are the same to simplify this

were described for a Three-Pool kinetic model. $K_{pl}(t)$, and $K_{lp}(t)$ are correction terms in our

Pyruvate $\underset{K_{ip}}{\overset{K_{ei}}{\rightleftharpoons}}$ Pyruvate $\underset{K_{ip}}{\overset{K_{pl}}{\rightleftharpoons}}$ Lactate



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Fig. 2 This THP1 cell data was irradiated by 13	³⁷ Cs. Dynamic data comparison between our
model, traditional model and cell experiment.	(a) The dynamic data, blue dot, represents the
extracellular and intracellular signal of 13C pyr	ruvate in the cell experiment. The orange dot
represents our model. The green dot represer	nts traditional model. (b) The dynamic data
points represents the intracellular signal of 130	C Lactate in the cell experiment (blue), our

Table 1 The conversion rates and correction term were fitted by our model. The cells has two groups. One was imaged after irradiated by ¹³⁷Cs. The other was imaged directly without radiation. The signal in the radiation group corresponded to Fig. 2. The signal in the non-radiation group corresponded to Fig. 3.

		K _{pl} (x10 ⁻³) S ⁻¹	K _{lp} (x10 ⁻³) S ⁻¹
	Radiation	0.55(1-e ^{-t/36.7})	36.3(1-e ^{-t/36.7})
	Non-Radiation	0.33(1-e ^{-t/4.31})	15.9(1-e ^{-t/4.31})

CONCLUSIONS

The correction term in our three-pool model has fitted the experimental ¹³C Lactate data the same as the traditional model. However, only one set of data may not draw a conclusion for the correction term in our model. The further validation and the uncertainty of K_{pl} , K_{lp} , and T_{delay} of other datasets and comparison between our model and the traditional model are still needed.

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CONTACT INFORMATION

Ching-Yi Hsieh, PhD Email: chris11182016@gmail.com